



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

**NATIONAL/NASIONALE
SENIOR
CERTIFICATE/SERTIFIKAAT**

GRADE/GRAAD 12

MATHEMATICS P2/WISKUNDE V2

FEBRUARY/MARCH/FEBRUARIE/MAART 2017

MEMORANDUM

MARKS / PUNTE: 150

DEPARTMENT OF BASIC EDUCATION
PRIVATE BAG X895, PRETORIA 0001
 2017 -03- 16
APPROVED MARKING GUIDELINE
PUBLIC EXAMINATION

This memorandum consists of 21 pages.
Hierdie memorandum bestaan uit 21 bladsye.

Approved


Approved

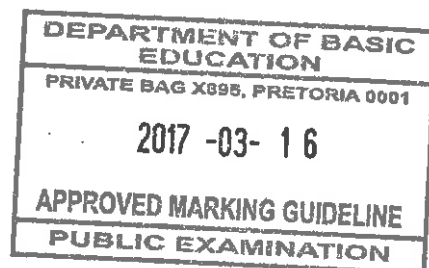
2017-03-16

NOTE:

- If a candidate answered a question TWICE, mark only the FIRST attempt.
- If a candidate has crossed out an attempt to answer a question and did not redo it, mark the crossed-out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

LET WEL:

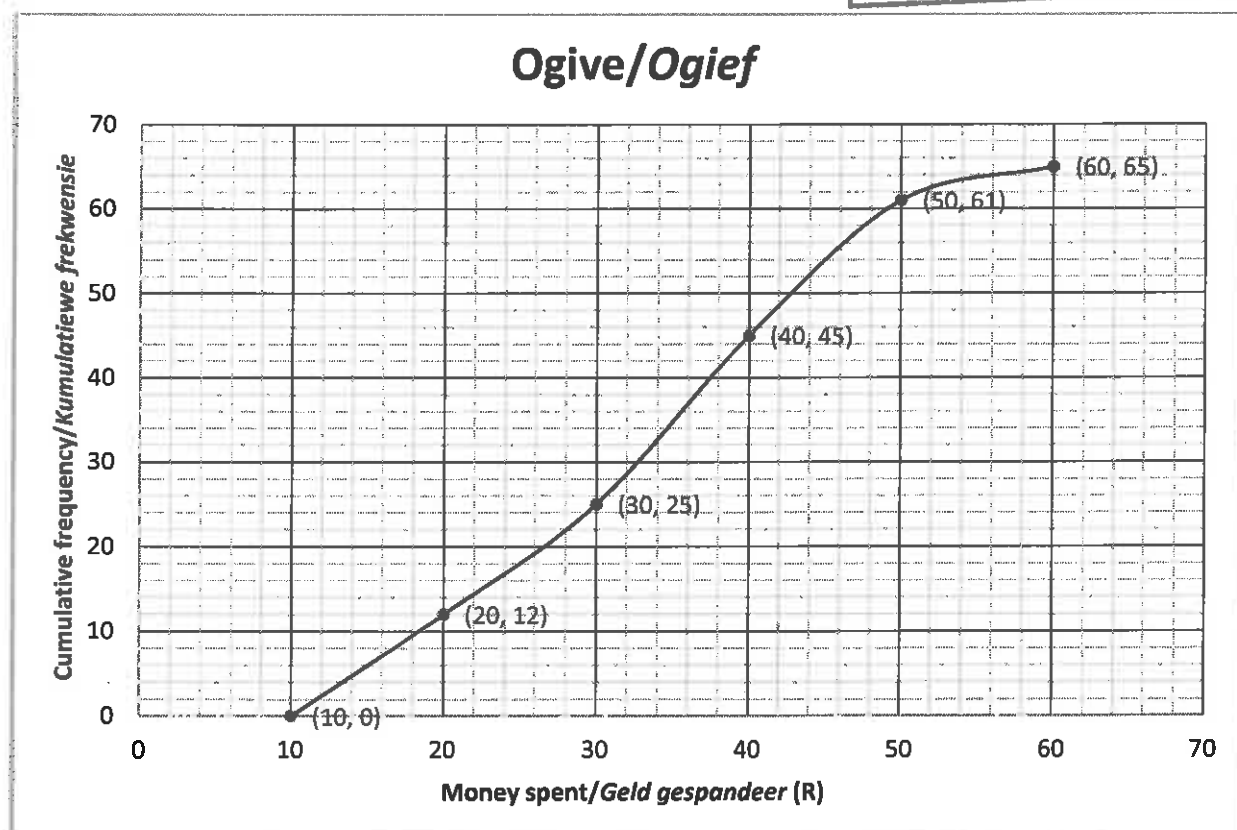
- *Indien 'n kandidaat 'n vraag TWEE keer beantwoord het, sien slegs die EERSTE poging na.*
- *As 'n kandidaat 'n poging om 'n vraag te beantwoord, doodgetrek en nie oorgedoen het nie, sien die doodgetrekte poging na.*
- *Volgehoue akkuraatheid is op ALLE aspekte van die memorandum van toepassing. Staak nasien by die tweede berekeningsfout.*
- *Om antwoorde/waardes om 'n probleem op te los, te veronderstel, word NIE toegelaat NIE.*



JP

[Signature]

QUESTION/VRAG 1



Amount of money/ Bedrag geld (in R)	$10 \leq x < 20$	$20 \leq x < 30$	$30 \leq x < 40$	$40 \leq x < 50$	$50 \leq x < 60$
Frequency Frekwensie	a	13	20	b	4

1.1	65 learners/leerders	✓ answer (1)
1.2	Modal class/Modale klas: $30 \leq x < 40$	✓ answer (1)
1.3	$a = 12$ $b = 61 - 45$ $= 16$	✓ answer ✓ answer (2)
1.4	No. of learners/Aantal leerders = $65 - 54$ OR/OF $65 - 55$ $= 11$ $= 10$ Answer only: full marks	✓ 54 or 55 ✓ 11 or 10 (2) [6]

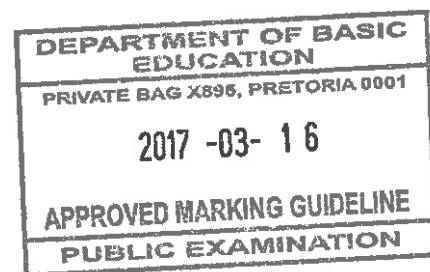
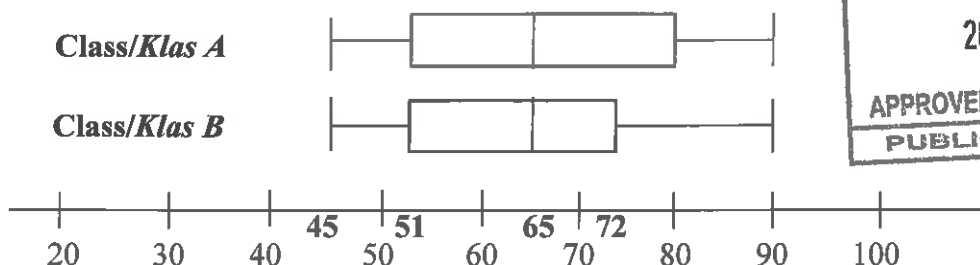
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QUESTION/VRAAG 2

2.1

Class/Klas A

Class/Klas B



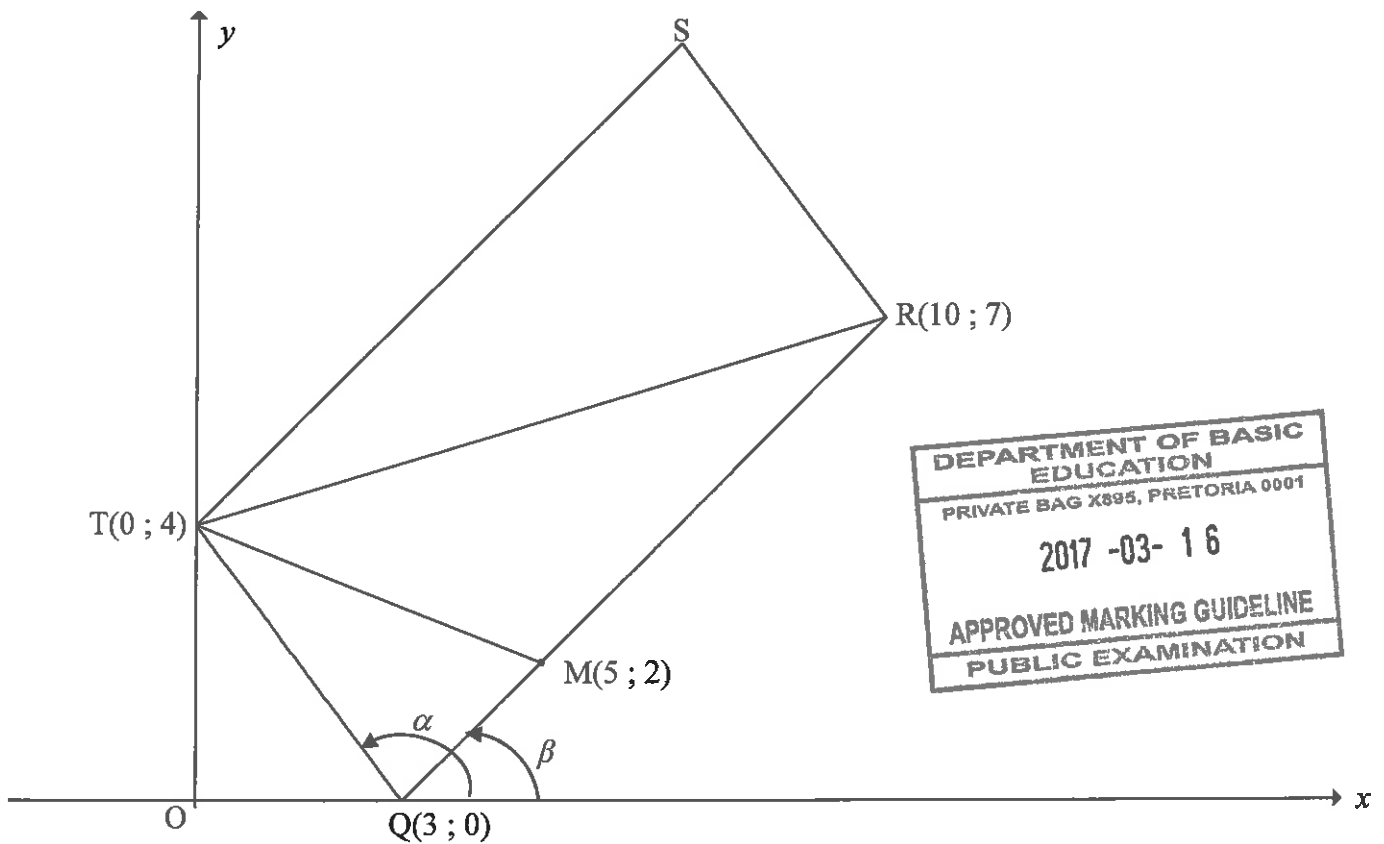
2.1.1	$\text{IQR of Class B/IKV van Klas B} = Q_3 - Q_1$ $= 72 - 51$ $= 21 \text{ marks/punte}$	✓ 72 and 51 ✓ 21 only (2)
2.1.2	Although the boxes contain the same number of data points, the marks for Class A are more widely spread./Alhoewel die monde dieselfde aantal datapunte bevat, is die punte van Klas A meer verspreid. OR/OF Although the boxes contain the same number of data points, the marks for Class B are more clustered./Alhoewel die monde dieselfde aantal datapunte bevat, is die punte van Klas B nader aan mekaar.	✓ ✓ Class A is more widely spread (2) ✓ ✓ Class B is more clustered (2)
2.1.3	Medians are the same/Mediane is dieselfde Ranges are the same OR Maximum and minimum values are the same/Variasiewydtes is dieselfde OF die maksimum en minimum waarde is dieselfde 75% of both classes obtained 51 and above/75% van albei klasse behaal 51 en meer.	✓ ✓ any TWO of the 3 reasons mentioned (2)

2.2

COUPLE/PAAR	1	2	3	4	5	6	7	8
JUDGE 1/ BEOORDELAAR 1	18	4	6	8	5	12	10	14
JUDGE 2/ BEOORDELAAR 2	15	6	3	5	5	14	8	15

2.2.1	$a = -0,03$ $b = 0,93$ $\hat{y} = -0,03 + 0,93x$	✓ value a ✓ value b ✓ equation (3)
2.2.2	$\hat{y} = -0,03 + 0,93(15)$ $= 13,92$ OR/OF 13,85 ≈ 14	✓ substitution ✓ answer (2)
2.2.3	Yes OR they are consistent, because $r = 0,9$. ($r = 0,89567\dots$)/Ja OF hulle is konsekwent, want $r = 0,9$. ($r = 0,89567\dots$)	✓ statement ✓ $r = 0,9$ (2) [13]

QUESTION/VRAAG 3



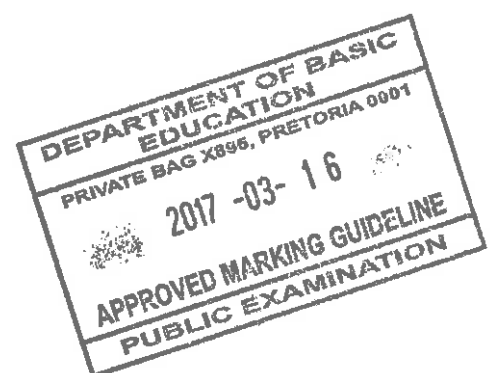
3.1	$m_{TQ} = \frac{4-0}{0-3}$ $= -\frac{4}{3}$	✓ answer (1)
3.2	$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $RQ = \sqrt{(10-3)^2 + (7-0)^2}$ $RQ = \sqrt{98} = 7\sqrt{2}$	✓ substitution/substitusie ✓ answer in surd form (2)
3.3	$m_{FQ} = m_{TQ}$ $\frac{-8}{k-3} = \frac{4}{3}$ $4k - 12 = 24$ $k = 9$ OR/OF $m_{FT} = m_{QT}$ $\frac{-8-4}{k-0} = \frac{4}{3}$ $-36 = -4k$ $k = 9$ OR/OF Equation of TQ: $y = -\frac{4}{3}x + 4$ $-8 = -\frac{4}{3}k + 4$ $k = 9$	✓ equating gradients/stel gradient gelyk ✓ $m_{FQ} = \frac{-8}{k-3}$ ✓ simplification/vereenvoudig ✓ answer (4)

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3.4	Using transformation/<i>Gebruik transformasie</i>: $\therefore S(7 ; 11)$ OR/OF Midpoint of TR = midpoint of SQ [diag m/hkle m] Midpoint of TR = $(5 ; \frac{11}{2})$ $\frac{x_S + 3}{2} = 5$ and $\frac{y_S + 0}{2} = \frac{11}{2}$ $\therefore x_S = 7$ and $y_S = 11$ $\therefore S(7 ; 11)$ OR/OF Equation of TS: $y = \left(\frac{7-2}{10-5}\right)x + 4 = x + 4$ Equation of RS: $y - 7 = -\frac{4}{3}(x - 10)$ $y = -\frac{4}{3}x + \frac{61}{3}$ $x + 4 = -\frac{4}{3}x + \frac{61}{3}$ $7x = 49$ $x = 7$ $\therefore y = 11$ $\therefore S(7 ; 11)$	✓ ✓ x-value/waarde ✓ ✓ y-value/waarde (4) ✓ x-value/waarde of/van T ✓ y-value/waarde of/van T ✓ x-value/waarde of/van S ✓ y-value/waarde of/van S (4) ✓ equations of TS and RS/vgl's van TS en RS ✓ equating / gelykstel ✓ x-value/waarde ✓ y-value/waarde (4)
3.5	$\hat{T}\hat{S}R = \hat{T}\hat{Q}R$ [opp $\angle$s of m/teenoorst $\angle$e m] $\hat{T}\hat{Q}R = \alpha - \beta$ $\tan \alpha = m_{TQ} = -\frac{4}{3}$ $\therefore \alpha = 180^\circ - 53,13^\circ = 126,87^\circ$ $\tan \beta = m_{RQ} = \frac{7}{7} = 1$ $\therefore \beta = 45^\circ$ $\hat{T}\hat{Q}R = 126,87^\circ - 45^\circ$ $= 81,87^\circ$ $\hat{T}\hat{S}R = 81,87^\circ$ OR/OF	✓ $\hat{T}\hat{Q}R = \alpha - \beta$ ✓ $\tan \alpha = m_{TQ}$ ✓ α ✓ $\tan \beta = m_{RQ}$ ✓ β ✓ answer (6)

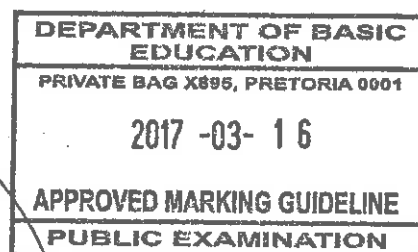
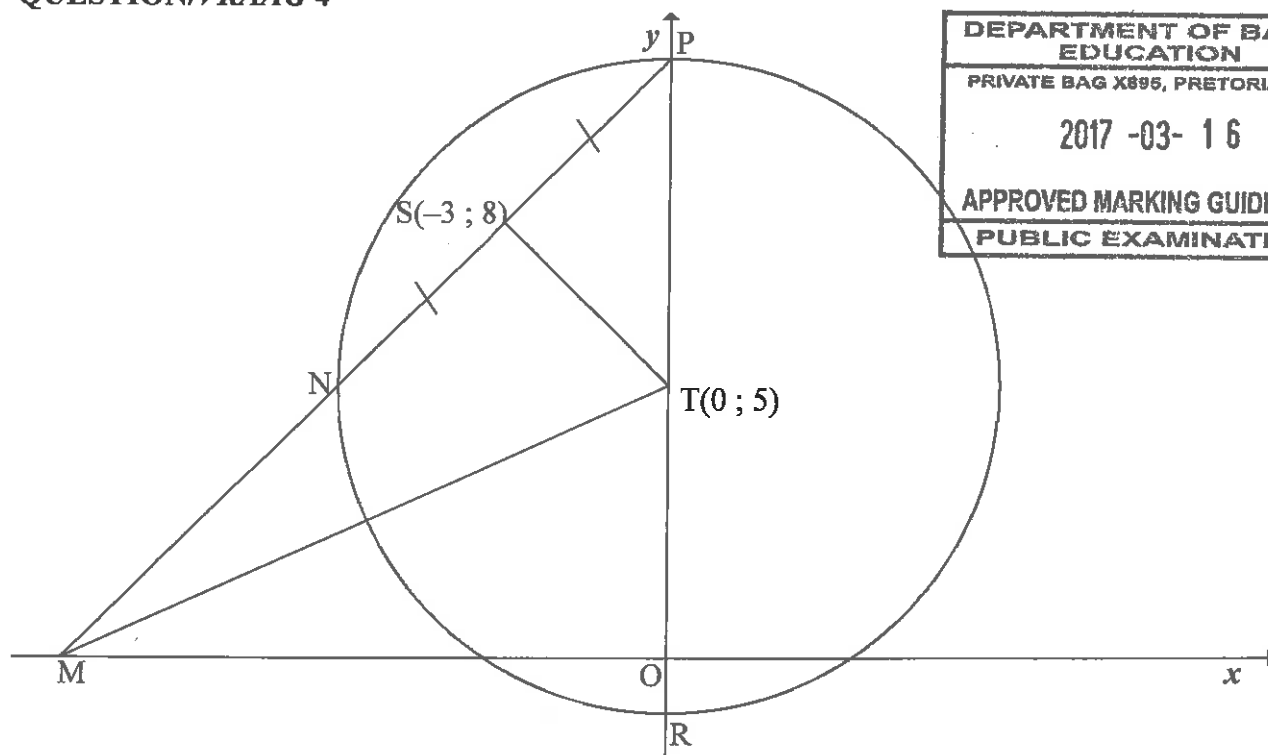
	$TQ = SR = 5$ $TR = \sqrt{100 + 9} = \sqrt{109}$ $RQ = TS = \sqrt{49 + 49} = \sqrt{98}$ $\cos R\hat{Q}T = \cos T\hat{S}R = \frac{TQ^2 + RQ^2 - TR^2}{2 \cdot TQ \cdot RQ}$ $= \frac{25 + 98 - 109}{2(5)(\sqrt{98})}$ $= 0,141...$ $R\hat{Q}T = T\hat{S}R = 81,87^\circ$	✓ length of TQ OR SR ✓ length of TR ✓ length of RQ OR TS ✓ correct subst into cosine rule ✓ simplification ✓ answer
3.6.1	$MQ = \sqrt{(5-3)^2 + (2-0)^2}$ $MQ = \sqrt{8}$ $\frac{MQ}{RQ} = \frac{\sqrt{8}}{\sqrt{98}}$ $= \frac{2}{7} \quad \text{or} \quad 0,29$ Answer only: full marks	✓ substitution/ <i>substitusie</i> ✓ $MQ = \sqrt{8} = 2\sqrt{2}$ ✓ answer
3.6.2	$\frac{\text{area of } \Delta TQM}{\text{area of } \Delta TQR} = \frac{\frac{1}{2} \cdot QM \cdot \perp h}{\frac{1}{2} \cdot QR \cdot \perp h} \quad [\perp h \text{ same/dieselfde}]$ $= \frac{QM}{QR} = \frac{2}{7}$ $\frac{\text{area of } \Delta TQM}{\text{area of parm RQTS}} = \frac{\text{area of } \Delta TQM}{2 \times \text{area of } \Delta TQR}$ $\frac{1}{2} \left(\frac{2}{7} \right) = \frac{1}{7}$ 2017-03-16 APPROVED MARKING GUIDELINE PUBLIC EXAMINATION $\frac{\text{area of } \Delta TQM}{\text{area of } \Delta TQR} = \frac{QM}{QR}$ $= \frac{2}{7}$ $\frac{\text{area of } \Delta TQM}{\text{area of parm RQTS}} = \frac{\text{area of } \Delta TQM}{2 \text{area of } \Delta TQR}$ $= \frac{1}{2} \left(\frac{2}{7} \right) = \frac{1}{7}$	✓ $\frac{\text{area of } \Delta TQM}{\text{area of } \Delta TQR} = \frac{2}{7}$ ✓ area parm RQTS = 2area ΔTQR ✓ answer
	$\frac{\text{area of } \Delta TQM}{\text{area of } \Delta TQR} = \frac{QM}{QR}$ $= \frac{2}{7}$ $\frac{\text{area of } \Delta TQM}{\text{area of parm RQTS}} = \frac{\text{area of } \Delta TQM}{2 \text{area of } \Delta TQR}$ $= \frac{1}{2} \left(\frac{2}{7} \right) = \frac{1}{7}$	✓ $\frac{\text{area of } \Delta TQM}{\text{area of } \Delta TQR} = \frac{2}{7}$ ✓ area parm RQTS = 2area ΔTQR ✓ answer

$\frac{\text{area of } \triangle TQM}{\text{area of parm RQTS}} = \frac{\frac{1}{2} QM \cdot \perp h}{RQ \cdot \perp h}$ $= \frac{1}{2} \left(\frac{2}{7} \right)$ $= \frac{1}{7}$ OR/OF $\frac{\text{area of } \triangle TQM}{\text{area of parm RQTS}} = \frac{\frac{1}{2} QT \cdot QM \cdot \sin(\alpha - \beta)}{2 \text{area of } \triangle QTR}$ $= \frac{\frac{1}{2} QT \cdot QM \cdot \sin(\alpha - \beta)}{2 \left[\frac{1}{2} \cdot QT \cdot QR \cdot \sin(\alpha - \beta) \right]}$ $= \frac{1}{2} \left(\frac{2}{7} \right)$ $= \frac{1}{7}$	$\checkmark \frac{\frac{1}{2} QM \cdot \perp h}{RQ \cdot \perp h}$ $\checkmark \frac{1}{2} \left(\frac{2}{7} \right)$ $\checkmark \text{ answer}$ (3) $\checkmark$ $\text{area parm RQTS} = 2 \text{area } \triangle TQR$ $\checkmark \frac{\frac{1}{2} QT \cdot QM \cdot \sin(\alpha - \beta)}{2 \left[\frac{1}{2} \cdot QT \cdot QR \cdot \sin(\alpha - \beta) \right]}$ $\checkmark \text{ answer}$ (3) [23]
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QUESTION/VRAAG 4

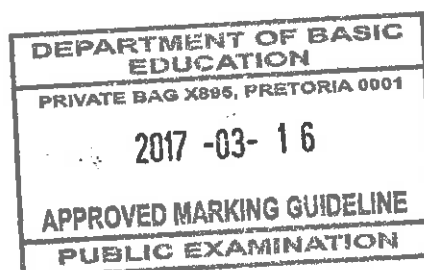


4.1	line from centre to midpt of chord / <i>lyn vanaf midpt na midpt van koord</i>	✓ answer (1)
4.2	$m_{ST} = \frac{8-5}{-3-0}$ $= -1$ $m_{ST} \times m_{NP} = -1 \quad [TS \perp NP]$ $\therefore m_{NP} = 1$ $\therefore y = x + c$ $8 = -3 + c$ $c = 11$ $\therefore y = x + 11$ OR/OF $y - y_1 = 1(x - x_1)$ $y - 8 = 1(x + 3)$ $y = x + 11$	✓ subst (-3 ; 8) and (0 ; 5) into gradient formula ✓ m_{ST} ✓ m_{NP} ✓ subst (-3 ; 8) into equation of a line ✓ equation (5)
4.3	P(0 ; 11) [y-intercept of chord NP] $\therefore$ radius is 6 units R(0 ; -1) Equations of the tangents to the circle parallel to the x-axis/ <i>Vgls van die raaklyne aan die sirkel aan die x-as:</i> $y = 11$ and $y = -1$	✓ coordinates of P/ koördinate v P ✓ coordinates of R koördinate van R ✓✓ answers (4)
4.4	M(-11 ; 0) [x-intercept of/x-afsnit van NP] $MT = \sqrt{(0 - 11)^2 + (5 - 0)^2}$ $MT = \sqrt{146} = 12,08$	✓✓ coordinates of M ✓ substitution ✓ answer (4)

4.5	MT = diameter/middel lyn [conv $\angle$ in $\frac{1}{2}$ circle/omgek $\angle$ in $\frac{1}{2}$ sirkel] radius = $\frac{\sqrt{146}}{2}$ units Centre of circle/Middelpunt v sirkel = Midpoint MT /Middelpunt MT = $\left(\frac{-11}{2}; \frac{5}{2}\right)$ Equation of circle through S, T and M: $\left(x + \frac{11}{2}\right)^2 + \left(y - \frac{5}{2}\right)^2 = \frac{146}{4}$ OR/OF $\left(x + 5\frac{1}{2}\right)^2 + \left(y - 2\frac{1}{2}\right)^2 = \frac{73}{2} = 6,04$	✓ radius of circle ✓ x value of M ✓ y value of M ✓ LHS of equation ✓ RHS of equation (5) [19]
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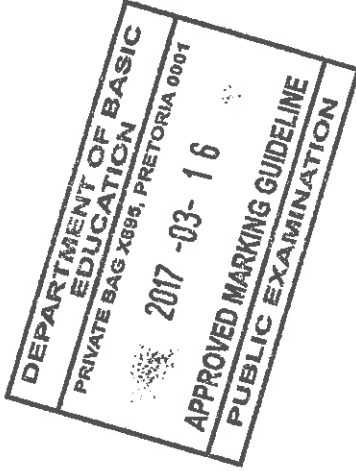
QUESTION/VRAAG 5

5.1	$a = -1$ $b = 2$	✓ answer ✓ answer (2)
5.2	$f(3x) = -\sin 3x$ Period of $f(3x) = \frac{360^\circ}{3}$ $= 120^\circ$ Answer only: Full marks	✓ $\frac{360^\circ}{3}$ ✓ answer (2)
5.3	$x \in [90^\circ; 135^\circ) \cup \{180^\circ\}$ OR/OF $90^\circ \leq x < 135^\circ$ or $x = 180^\circ$	✓ 90° and 135° in interval form ✓ 180° as single value ✓ correct brackets (3) ✓ 90° and 135° in interval form ✓ 180° as single value ✓ correct inequalities (3) [7]



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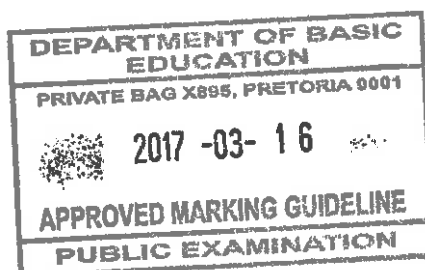
QUESTION/VRAAG 6

6.1.1	$\sin(360^\circ - 36^\circ) = -\sin 36^\circ$	✓ answer (1)
6.1.2	$\cos 72^\circ = \cos(2 \times 36^\circ)$ $= 1 - 2 \sin^2 36^\circ$ Answer only: Full marks	✓ double angle/dubbelhoek ✓ answer (2)
6.2	R.T.P.: $1 - \frac{\tan^2 \theta}{1 + \tan^2 \theta} = \cos^2 \theta$ LHS = $\frac{1 + \tan^2 \theta - \tan^2 \theta}{1 + \tan^2 \theta}$ $= \frac{1}{1 + \frac{\sin^2 \theta}{\cos^2 \theta}}$ $= \frac{1}{\frac{\cos^2 \theta + \sin^2 \theta}{\cos^2 \theta}}$ $= \frac{1}{\frac{1}{\cos^2 \theta}}$ $= \cos^2 \theta$ $= \text{RHS}$ OR/OF LHS = $\frac{1 + \tan^2 \theta - \tan^2 \theta}{1 + \tan^2 \theta}$ $= \frac{1}{1 + \frac{\sin^2 \theta}{\cos^2 \theta}}$ $= \frac{1}{1 + \frac{\sin^2 \theta}{\cos^2 \theta}} \times \frac{\cos^2 \theta}{\cos^2 \theta}$ $= \frac{\cos^2 \theta}{\cos^2 \theta + \sin^2 \theta}$ $= \frac{\cos^2 \theta}{1}$ $= \cos^2 \theta$ $= \text{RHS}$ 	✓ writing as a single fraction/skryf as enkelbreuk ✓ quotient identity/kwosiëntidentiteit ✓ denominator as a single fraction / Noemer as enkelbreuk ✓ square identity/vierkantidentiteit (4)
		✓ writing as a single fraction/skryf as enkelbreuk ✓ quotient identity / kwosiëntidentiteit ✓ $\times \frac{\cos^2 \theta}{\cos^2 \theta}$ ✓ square identity/vierkantidentiteit (4)

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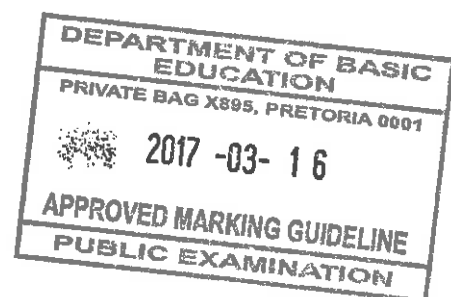
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	OR/OF $\text{LHS} = 1 - \left(\frac{\sin^2 \theta}{\cos^2 \theta} \div \left(1 + \frac{\sin^2 \theta}{\cos^2 \theta} \right) \right)$ $= 1 - \left(\frac{\sin^2 \theta}{\cos^2 \theta} \times \frac{\cos^2 \theta}{\cos^2 \theta + \sin^2 \theta} \right)$ $= 1 - \left(\frac{\sin^2 \theta}{\cos^2 \theta} \times \frac{\cos^2 \theta}{1} \right)$ $= 1 - \sin^2 \theta$ $= \cos^2 \theta$ $= \text{RHS}$	✓ quotient identity/ <i>kwosiëntidentiteit</i> ✓ writing as a single fraction/ <i>as enkelbreuk</i> ✓ square identity/<i>vierkantidentiteit</i> ✓ simplification/<i>vereenvoudiging</i> (4)
6.3	$\cos^2 \frac{1}{2}x = \frac{1}{4}$ $\cos \frac{1}{2}x = \frac{1}{2} \text{ or } -\frac{1}{2}$ $\frac{1}{2}x = 60^\circ + k.360^\circ \text{ or } \frac{1}{2}x = 300^\circ + k.360^\circ \text{ or}$ $\frac{1}{2}x = 120^\circ + k.360^\circ \text{ or } \frac{1}{2}x = 240^\circ + k.360^\circ$ $x = 120^\circ + k.720^\circ \text{ or } x = 600^\circ + k.720^\circ \text{ or}$ $x = 240^\circ + k.720^\circ \text{ or } x = 480^\circ + k.720^\circ; k \in \mathbb{Z}$ OR/OF $\cos^2 \frac{1}{2}x = \frac{1}{4}$ $\cos \frac{1}{2}x = \frac{1}{2} \text{ or } -\frac{1}{2}$ $\frac{1}{2}x = \pm 60^\circ + k.360^\circ \text{ or } \frac{1}{2}x = \pm 120^\circ + k.360^\circ$ $x = \pm 120^\circ + k.720^\circ \text{ or } x = \pm 240^\circ + k.720^\circ; k \in \mathbb{Z}$	✓✓ $\cos^2 \frac{1}{2}x = \frac{1}{4}$ ✓ 60° and 300° ✓ 120° and 240° ✓ write at least one general solution as $\frac{1}{2}x = \angle + k.360^\circ$ ✓ write at least one general solution as $x = \angle + k.720^\circ; k \in \mathbb{Z}$ (6) ✓✓ $\cos^2 \frac{1}{2}x = \frac{1}{4}$ ✓ $\pm 60^\circ$ ✓ $\pm 120^\circ$ ✓ write at least one general solution as $\frac{1}{2}x = \angle + k.360^\circ$ ✓ write at least one general solution as $x = \angle + k.720^\circ k \in \mathbb{Z}$ (6)



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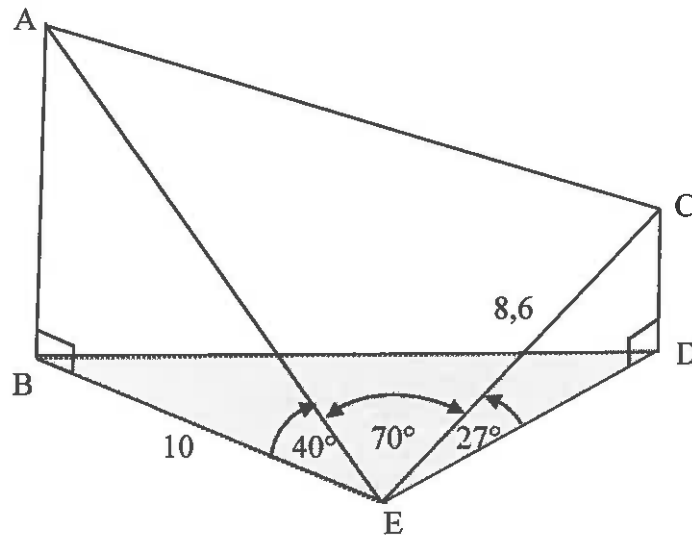
6.4.1	$\sin(A - B) = \cos[90^\circ - (A - B)]$ $= \cos[(90^\circ - A) - (-B)]$ $= \cos(90^\circ - A)\cos(-B) + \sin(90^\circ - A)\sin(-B)$ $= \sin A \cos B + \cos A(-\sin B)$ $= \sin A \cos B - \cos A \sin B$ OR/OF $\sin(A - B) = \cos[90^\circ - (A - B)]$ $= \cos[(90^\circ + B) - A]$ $= \cos(90^\circ + B)\cos A + \sin(90^\circ + B)\sin A$ $= -\sin B \cos A + \cos B \sin A$ $= \sin A \cos B - \cos A \sin B$	✓ co-ratio/ko-verhouding ✓ writing as a difference of A & B/ <i>skryf as verskil van A & B</i> ✓ expansion/uitbreiding ✓ all reductions/alle reduksies (4)
6.4.2	$\sin(x + 64^\circ) \cos(x + 379^\circ) + \sin(x + 19^\circ) \cos(x + 244^\circ)$ $= \sin(x + 64^\circ) \cos(x + 19^\circ) + \sin(x + 19^\circ)[- \cos(x + 64^\circ)]$ $= \sin(x + 64^\circ) \cos(x + 19^\circ) - \cos(x + 64^\circ) \sin(x + 19^\circ)$ $= \sin[x + 64^\circ - (x + 19^\circ)]$ $= \sin 45^\circ$ $= \frac{1}{\sqrt{2}}$	✓ $\cos(x + 379^\circ) = \cos(x + 19^\circ)$ ✓✓ $\cos(x + 244^\circ) = -\cos(x + 64^\circ)$ ✓✓ compound formula identity/ <i>saamgestelde identiteit</i> ✓ $\sin 45^\circ$ (6)

[23]

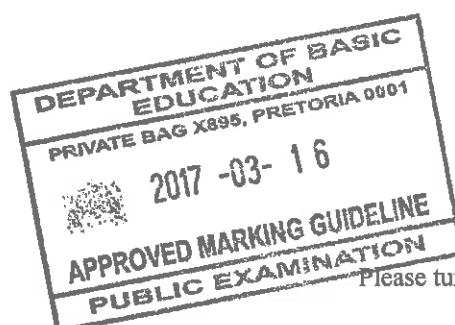
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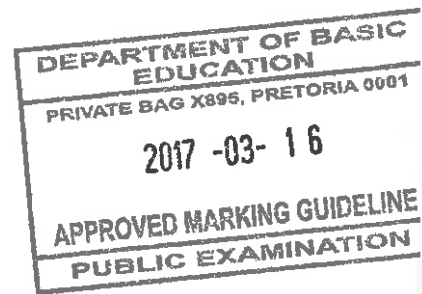
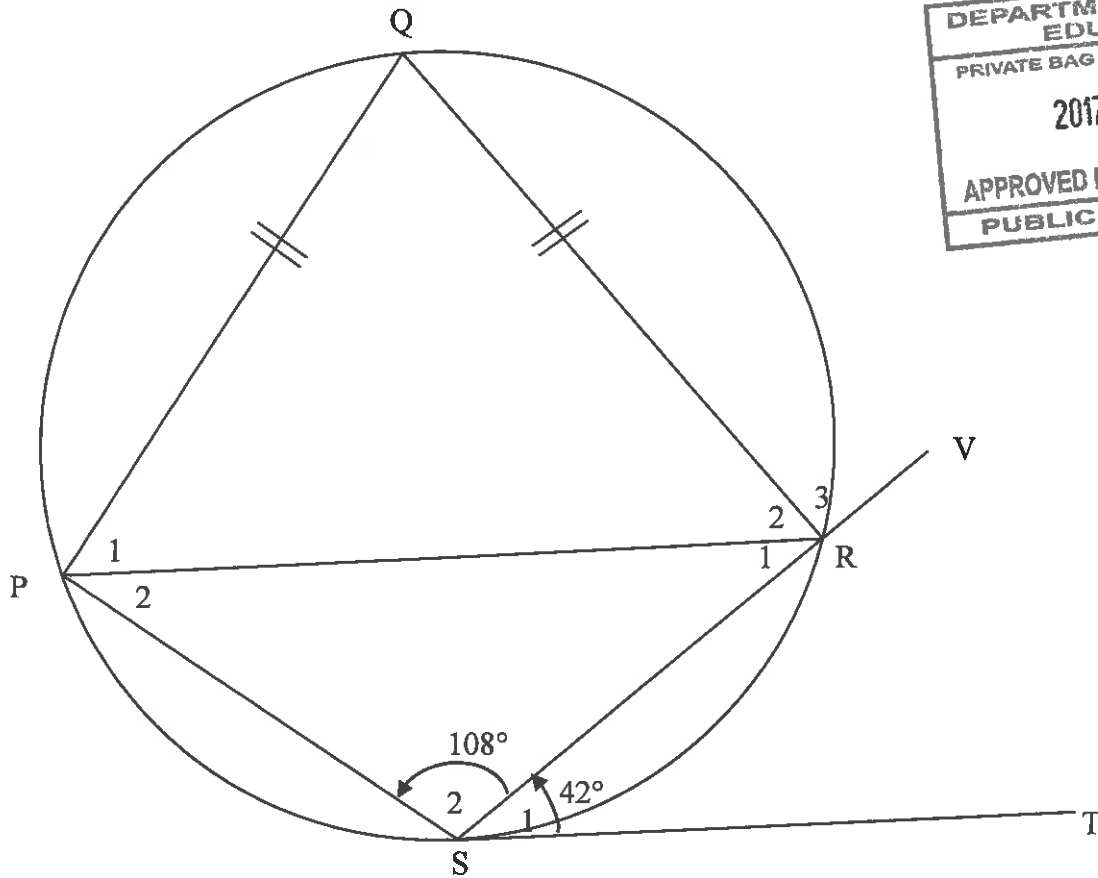
QUESTION/VRAAG 7



7.1	$\sin 27^\circ = \frac{CD}{8,6}$ $CD = 8,6 \sin 27^\circ$ $CD = 3,90 \text{ m}$	✓ substitution in correct trig ratio / <i>substitusie in korrekte trig verh</i> ✓ answer (2)
7.2	$\cos 40^\circ = \frac{10}{AE}$ $AE = \frac{10}{\cos 40^\circ}$ $AE = 13,05 \text{ m}$	✓ substitution in correct trig ratio / <i>substitusie in korrekte trig verh</i> ✓ answer (2)
7.3	$AC^2 = CE^2 + AE^2 - 2 CE \cdot AE (\cos \hat{AEC})$ $= (8,6)^2 + (13,05)^2 - 2(8,6)(13,05)(\cos 70^\circ)$ $= 167,49$ $AC = 12,94 \text{ m}$	✓ correct use of cosine rule in $\triangle ACE$ / <i>korrekte gebruik van reel in $\triangle ACE$</i> ✓ correct subst into cosine rule ✓ AC^2 ✓ answer (4) [8]



QUESTION/VRAAG 8

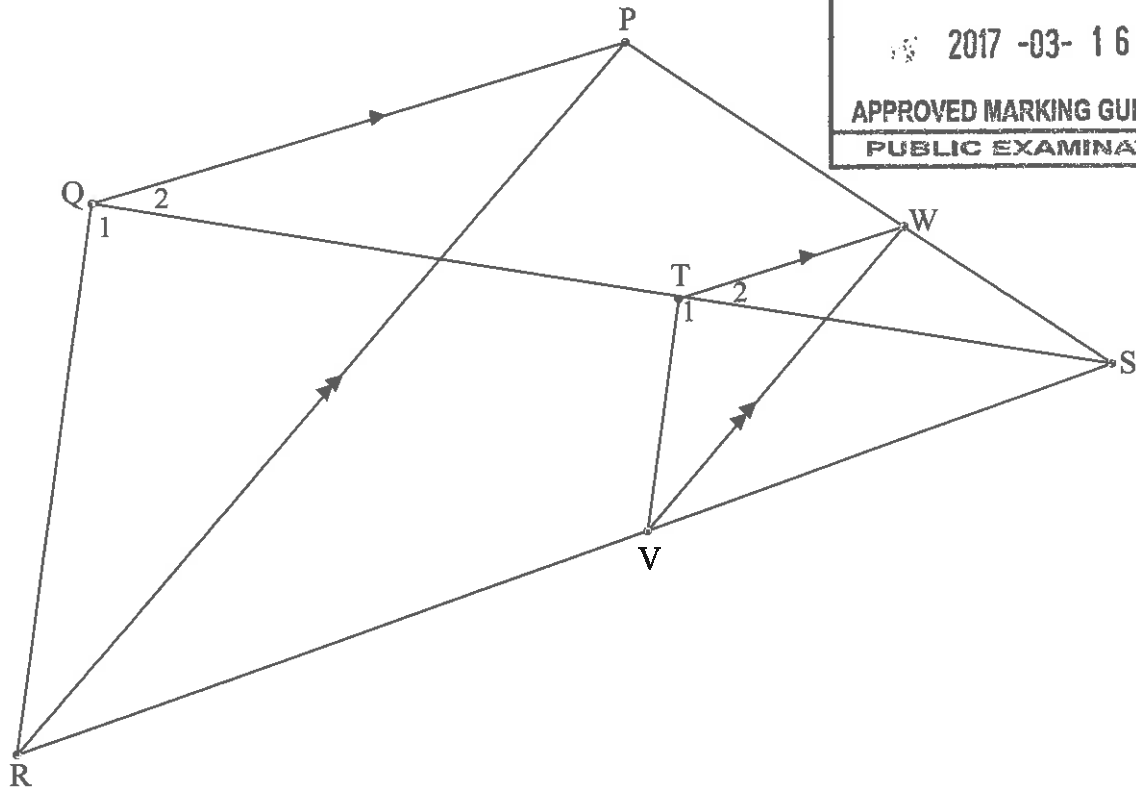
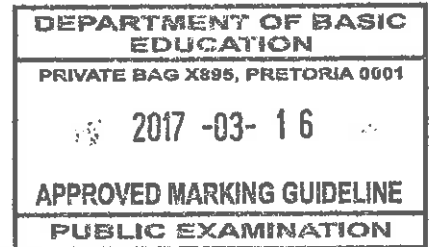


8.1	$\hat{Q} = 72^\circ$ [opp $\angle$ s of cyclic quad/teenoorst $\angle$ e koordevh]	✓ S ✓ R (2)
8.2	$\hat{R}_2 = \hat{P}_1$ [$\angle$ s opp equal sides/ $\angle$ e teenoor gelyke sye] $\hat{R}_2 = \frac{180^\circ - 72^\circ}{2}$ [sum of $\angle$ s in Δ /som v $\angle$ e in Δ] $= 54^\circ$	✓ S/R ✓ answer (2)
8.3	$\hat{P}_2 = 42^\circ$ [tan chord theorem/raakl-koordst]	✓ S ✓ R (2)
8.4	$\hat{R}_3 = \hat{P}_1 + \hat{P}_2$ [ext $\angle$ of cyclic quad/buite $\angle$ van koordevh] $= 54^\circ + 42^\circ$ $= 96^\circ$ OR/OF $\hat{R}_1 = 180^\circ - 108^\circ - 42^\circ = 30^\circ$ [sum of/som van $\angle$ s/e in Δ] $\hat{R}_3 = 180^\circ - \hat{R}_1 - \hat{R}_2$ [$\angle$ s on str line/ $\angle$ e op reguitlyn] $= 180^\circ - 30^\circ - 54^\circ$ [sum of/som van $\angle$ s/e in Δ] $= 96^\circ$	✓ R ✓ S (2) ✓ $\hat{R}_1 = 30^\circ$ ✓ S (2) [8]

PP

[Signature]

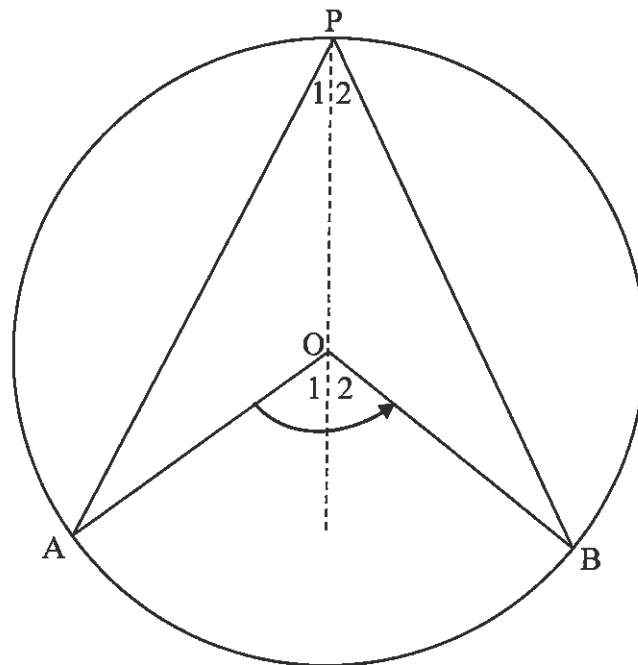
QUESTION/VRAAG 9



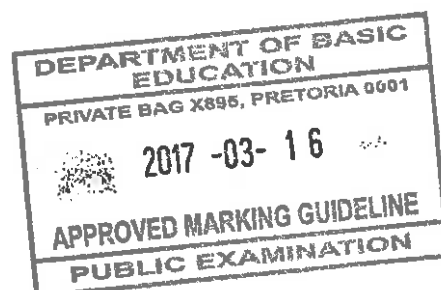
9.1.1	$\frac{ST}{TQ} = \frac{SW}{WP}$ $= \frac{2}{3}$	[prop theorem/eweredighst; TW QP] ✓ S ✓ S	(2)
9.1.2	$\frac{SV}{VR} = \frac{SW}{WP}$ $= \frac{2}{3}$	[prop theorem/eweredighst; VW RP] ✓ answer	(1)
9.2	$\frac{ST}{TQ} = \frac{SV}{VR}$ ∴ TV QR [both equal/beide gelyk $\frac{WS}{PW}$] [line divides 2 sides of Δ in prop/lyn verdeel 2 sye van Δ in dies verh] ∴ $\hat{T}_1 = \hat{Q}_1$ [corresp/ooreenkomst ∠s/e; TV QR]	✓ S ✓ S ✓ R ✓ R	(4)
9.3	ΔVWS ΔRPS	✓ ΔRPS (any order)	(1)
9.4	$\frac{WV}{PR} = \frac{SW}{SP}$ $= \frac{2}{5}$ OR/OF $\frac{WV}{PR} = \frac{SV}{SR}$ $= \frac{2}{5}$	[ΔVWS ΔRPS] [ΔVWS ΔRPS] ✓ ratio ✓ answer	(2) [10]

QUESTION/VRAAG 10

10.1



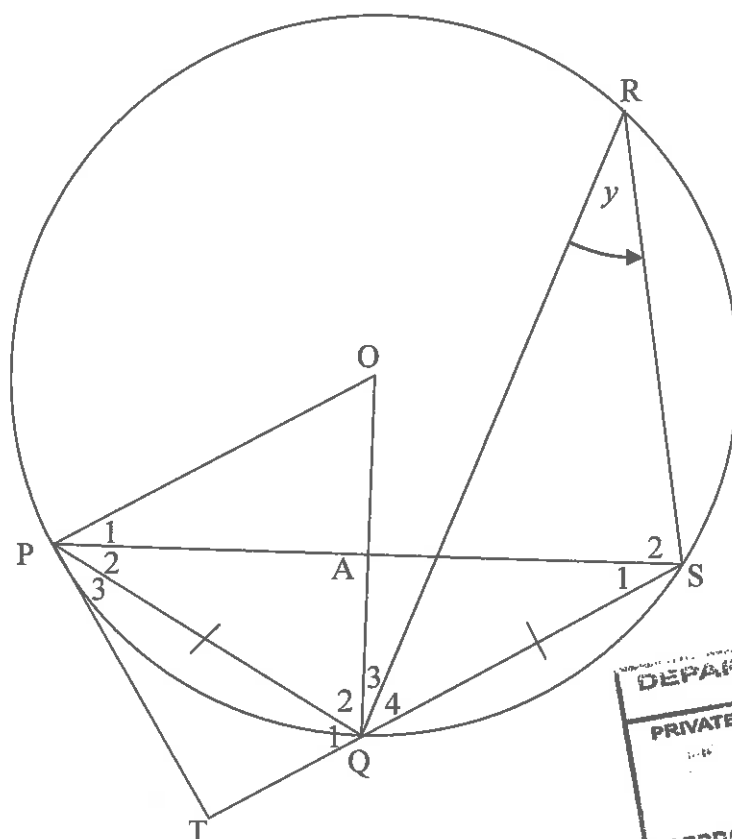
Constr/Konst :	✓ construction
Draw line PO and extend /Trek lyn PO en verleng	
Proof/Bewys :	
OP = OA [radii]	
$\therefore \hat{P}_1 = \hat{A}$ [$\angle$ s opp/teenoor = sides/sye]	✓ S/R
but $\hat{O}_1 = \hat{P}_1 + \hat{A}$ [ext $\angle$ of Δ]	✓ S/R
$\therefore \hat{O}_1 = 2\hat{P}_1$	✓ S
Similarly/Netso, $\hat{O}_2 = 2\hat{P}_2$	
$\therefore \hat{O}_1 + \hat{O}_2 = 2(\hat{P}_1 + \hat{P}_2)$	✓ S
i.e. $\hat{A}\hat{O}\hat{B} = 2\hat{A}\hat{P}\hat{B}$	
(5)	



JP

Q

10.2

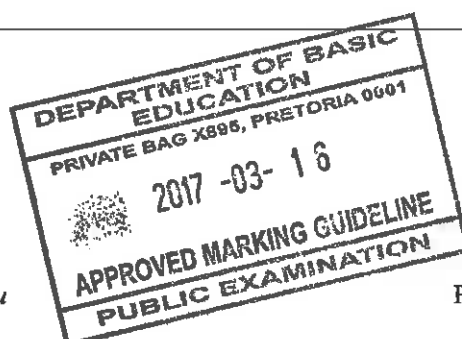


10.2.1	$\angle$ s in the same segment/ $\angle$ e in dieselfde sirkelsegment	✓ R (1)
10.2.2	$\hat{P}_2 = \hat{S}_1 = y$ [∠s opp equal sides/ $\angle$ e teenoor = sye] $\hat{S}_1 = \hat{P}_3 = y$ [tan chord theorem/raakl-koordst] $\therefore \hat{P}_2 = \hat{P}_3$ $\therefore PQ$ bisects $\hat{T}PS$	✓ S ✓ R ✓ S ✓ R (4)
10.2.3	$\hat{P}\hat{O}Q = 2\hat{S}_1 = 2y$ [∠at centre = $2 \times$ ∠at circ/midpts $\angle = 2 \times$ omtreks $\angle$]	✓ S ✓ R (2)
10.2.4	$\hat{T}PA = \hat{P}_2 + \hat{P}_3 = 2y$ [proved/bewys in 11.2.2] $\therefore \hat{T}PA = \hat{P}\hat{O}Q$ [proved/bewys in 11.2.3] $\therefore PT = \text{tangent}$ [converse tan chord theorem/omgek raakl-koordst]	✓ $\hat{T}PA = \hat{P}\hat{O}Q$ ✓ R (2)

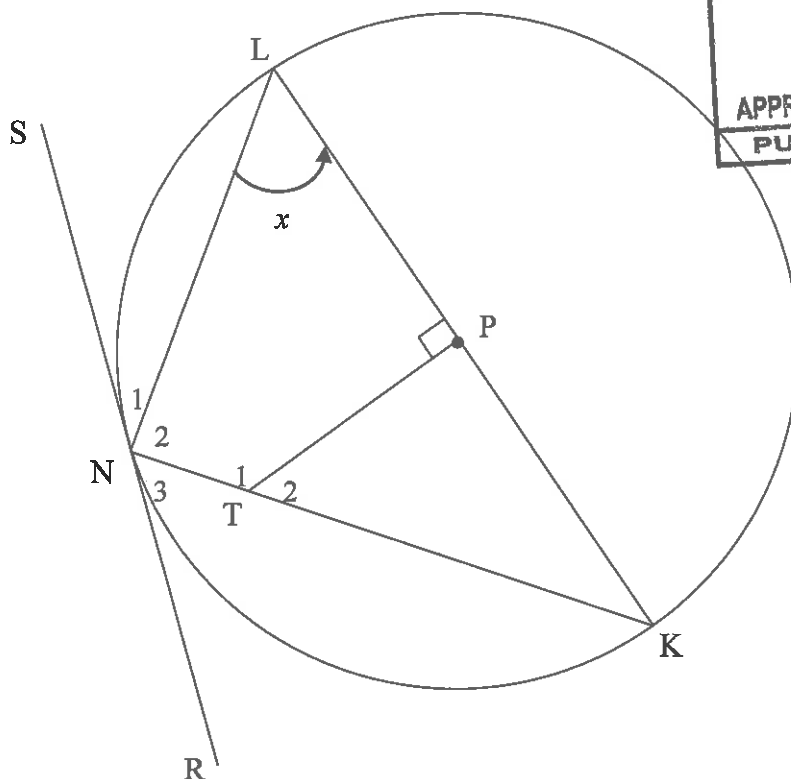
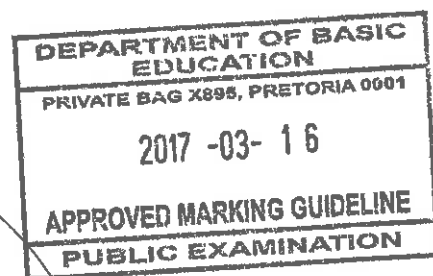
pp Q

10.2.5	$\widehat{OPQ} + \widehat{QOP} = 180^\circ - 2y$ [sum of/sum v $\angle$ s/e in Δ] $\therefore \widehat{OQP} = 90^\circ - y$ [$\angle$ s opp equal sides/ $\angle$ e to = sye; $OP = OQ$] In $\triangle PAQ$: $\widehat{OQP} + \widehat{P}_2 + \widehat{QAP} = 180^\circ$ $90^\circ - y + y + \widehat{QAP} = 180^\circ$ [sum of/sum v $\angle$ s/e in Δ] $\widehat{QAP} = 90^\circ$ $\therefore \widehat{OAP} = 90^\circ$ [$\angle$ s/e on straight line/op reguitlyn]	$\checkmark$ S $\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ S (5)
	OR/OF	
	$\widehat{OPT} = 90^\circ$ [radius $\perp$ tangent/raaklyn] $\therefore \widehat{P}_1 = 90^\circ - 2y$ $\widehat{P}_1 + \widehat{O} + \widehat{OAP} = 180^\circ$ [sum of/sum v $\angle$ s/e in Δ] $(90^\circ - 2y) + 2y + \widehat{OAP} = 180^\circ$ $\therefore \widehat{OAP} = 90^\circ$	$\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ S $\checkmark$ S (5)
	OR/OF	
	POSQ is a kite/'n vlieër $\therefore OQ \perp PS$ [diag of a kite/hoeklyne v vlieër] $\therefore \widehat{OAP} = 90^\circ$	$\checkmark\checkmark\checkmark$ S $\checkmark\checkmark$ R (5)
	OR/OF	
	In $\triangle OAP$ and $\triangle OAS$ $OP = OS$ (radii) OA is common $\widehat{POA} = 2y$ $= 2\widehat{P}_2$ $= \widehat{QOS}$ $\triangle OAP \equiv \triangle OAS$ (SAS) $\widehat{OAP} = \widehat{OAS}$ ($\equiv \Delta$ s) $\widehat{OAP} = \widehat{OAS} = 90^\circ$ ($\angle$ s on str line)	$\checkmark$ S $\checkmark$ S $\checkmark$ S $\checkmark$ R $\checkmark$ S (5)

[19]



QUESTION/VRAAG 11

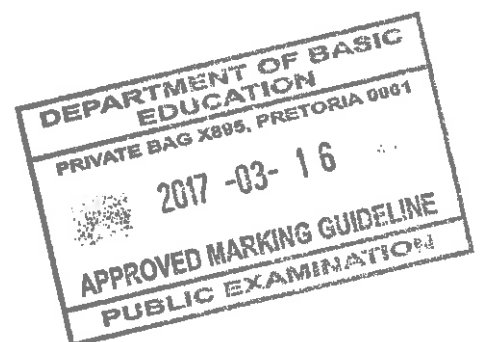


11.1	$\hat{N}_2 = 90^\circ$ [∠ in semi-circle/halfsirkel] $\therefore$ TPLN is a cyclic quad/ 'n koordevh [opp ∠s of quad is suppl/ teenoor ∠e v vh is suppl] OR $\hat{N}_2 = 90^\circ$ [∠ in semi-circle/halfsirkel] $\therefore$ TPLN is a cyclic quad [ext ∠ = int opp ∠/buite ∠ = to binne ∠]	✓ S ✓ R ✓ R (3)
11.2	$\hat{T}_2 = \hat{P}LN = x$ [ext ∠ of cyclic quad/buite ∠ van koordevh] $\hat{K} = 90^\circ - x$ [sum of/som v ∠s/e in Δ] $\hat{N}_1 = \hat{K} = 90^\circ - x$ [tan chord theorem/raakl-koordst] OR/OF $\hat{K} = 90^\circ - x$ [sum of/som v ∠s/e in Δ] $\hat{N}_1 = \hat{K} = 90^\circ - x$ [tan chord theorem/raakl-koordst] OR/OF $\hat{N}_3 = x$ [tan chord theorem/raakl-koordst] $\hat{N}_2 = 90^\circ$ [∠ in semi circle/ halfsirkel] $\hat{N}_1 = 90^\circ - x$ [straight line/reguitlyn]	✓ R ✓ S ✓ R (3) ✓ R ✓ S ✓ R (3) ✓ R ✓ S ✓ S (3)

JP

11.3.1	In $\triangle KTP$ and $\triangle KLN$: $\hat{P}KT = \hat{L}KN$ [common/<i>gemeen</i>] $\hat{K}PT = \hat{K}NL = 90^\circ$ [given/<i>gegee</i>] $\therefore \triangle KTP \parallel \triangle KLN$ [$\angle\angle\angle$] OR/OF In $\triangle KTP$ and $\triangle KLN$: $\hat{P}KT = \hat{L}KN$ [common/<i>gemeen</i>] $\hat{K}PT = \hat{K}NL = 90^\circ$ [given/<i>gegee</i>] $\hat{T}_2 = \hat{P}LN = x$ [proved in 11.2 OR sum of $\angle$s in $\triangle$] $\therefore \triangle KTP \parallel \triangle KLN$	✓ S ✓ S ✓ R (3)
11.3.2	$\frac{KT}{KL} = \frac{KP}{KN}$ [$\parallel \triangle$s] $\therefore KT \cdot KN = KP \cdot KL$ But $KL = 2KP$ [radii: $PK = LP$] $\therefore KT \cdot KN = KP \cdot 2KP$ $= 2KP^2$ $= 2(KT^2 - TP^2)$ [Theorem of Pythagoras] $= 2KT^2 - 2TP^2$	✓ S/R ✓ S ✓ S ✓ S ✓ S (5) [14]

TOTAL/TOTAAL: 150



ADDENDUM: MARCH 2017 PAPER 2

These notes are to be used in conjunction with the March 2017 Maths Paper 2 Marking memorandum.

Only persons who have been trained at a memo discussion for this paper will understand the background and application of these notes.

Question 1

1.2 Accept the following without any penalty: $30 < x \leq 40$ and $30 < x < 40$.

1.4 Answer only: full marks

Question 2

2.1.1 No CA if random values from the box and whisker diagram are used.

2.2.1 No penalty for incorrect rounding off. (1x OR $b < 0$ is not accepted)

Answer only: full marks

2.2.2 If no equation in 2.2.1 and answer only: 1/2

2.2.3 If the response is "No", then 0/2

Question 3

3.2 Answer must be in surd form as required. If surd form and then decimal answer is given, ignore the decimal answer.

If only decimal answer is given, then 1/2.

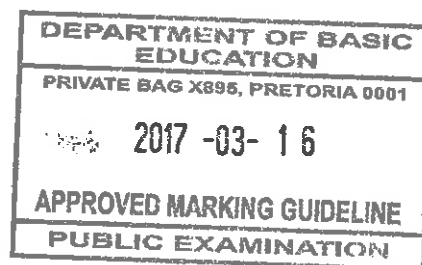
3.5 No penalty for incorrect rounding.

If candidate stops at $T\hat{Q}R = 81,87^\circ$, full marks.

Alternative:

$$m_{SR} = -\frac{4}{3} \quad \text{and} \quad m_{TS} = \frac{7-2}{10-5} = 1 \checkmark$$

$$\tan \hat{S} = \tan T\hat{Q}R = \tan(\alpha - \beta) \checkmark$$



Approved
P. M. Q.

Approved
C. M. Q.
2017-03-16

$$\begin{aligned}
 \tan(\alpha - \beta) &= \frac{\tan \alpha - \tan \beta}{1 + \tan \alpha \cdot \tan \beta} \quad \checkmark \\
 &= \frac{-\frac{4}{3} - 1}{1 + \left(-\frac{4}{3}\right)(1)} \quad \checkmark \\
 &= 7 \quad \checkmark \\
 \alpha - \beta &= 81,87^\circ \quad \checkmark
 \end{aligned}$$

3.6.1 Answer only – full marks

3.6.2 If candidates assume that QRST is a rectangle, then max 1/3.

Question 4

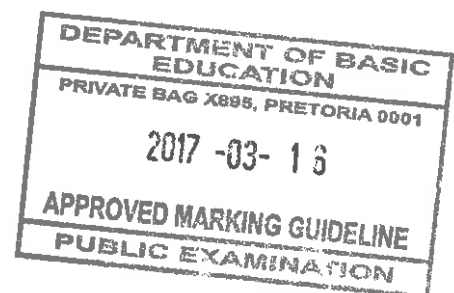
- 4.2 If candidates use the gradient of -1 , they then arrive at the equation of $y = -x + 5$. Award a max of 2/5.
- 4.3 If the equation in 4.2 is $y = -x + 5$ and the answer to 4.3 is $y = 5$, award 1/4. No marks for any other equations of tangents.
- 4.4 If the equation in 4.2 is $y = -x + 5$ and then calculate M to be $(5 ; 0)$ and then proceed to calculate MT to be $5\sqrt{2}$ or $\sqrt{50}$, then CA applies. Award 4/4.
- If the equation in 4.2 is $y = -x + 5$ and then change M to be $(-5 ; 0)$ and then proceed to calculate MT to be $5\sqrt{2}$ or $\sqrt{50}$, then a max of 2/4.
- 4.5 If M $(5 ; 0)$ is used, then CA applies. Award maximum of 5/5.
- If M $(-5 ; 0)$ is used, then award maximum of 4/5

Question 5

- 5.3 If answer is $90^\circ \leq x \leq 180^\circ$, then 0/3.
- If answer is $90^\circ; 135^\circ; 180^\circ$, then 1/3.

Question 6

- 6.4.2 1 mark for negative sign and 1 mark for $\cos(x + 64^\circ)$
- If there is an error in signs, max 4/6



Question 7

7.3 If there is a error in the sign in the cosine formula for $\triangle AEC$, then max 2/4.

The incorrect selection of the triangle, the incorrect application of the cosine formula or the use of the sine formula are breakdowns. Award 0/4.

GEOMETRY

- Remember: no marks can be allocated for a correct reason if the statement is incorrect.
- It is not acceptable to denote a composite angle as $\hat{B}_{2+3}$
- Markers must refer to the diagram when marking. Candidates may have answers on the diagram.

Question 8

8.2 Other than the reason given in the Examination guidelines, the following are acceptable:
base angles of isosceles triangle or isosceles triangle or $QP = QR$.

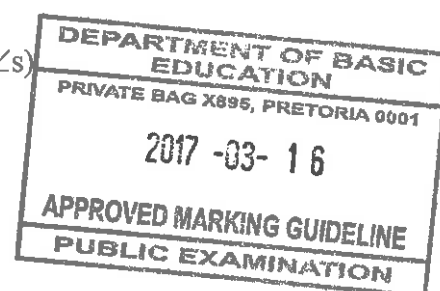
Question 9

9.1.1 If $\frac{ST}{TQ} = \frac{2}{3}$, award full marks.

9.2 No penalty for omitting parallel lines when stating corresponding angles are equal in the conclusion.

If no prove for $TV \parallel QR$, no marks for $\hat{T}_1 = \hat{Q}_1$ (corresponding $\angle$ s)

9.3 The order in which the triangle is written is not important.

**Question 10**

10.1 No evidence of construction, either on the diagram or in words, constitutes a break down: 0/5 marks.

Other than the reason given in the Examination guidelines, the following are acceptable:
base angles of isosceles triangle or isosceles triangle or $OP = OA$ or radii

10.2.1 Also accept subtended by same chord OR angles subtended by chord QS