

Instructions

There are **two** sections in this examination paper.

Section A	Concepts and Skills	150 marks	6 questions
Section B	Contexts and Applications	150 marks	3 questions

Answer **all nine** questions.

Write your answers in the spaces provided in this booklet. You may lose marks if you do not do so. There is space for extra work at the back of the booklet. You may also ask the superintendent for more paper. Label any extra work clearly with the question number and part.

The superintendent will give you a copy of the Formulae and Tables booklet. You must return it at the end of the examination. You are not allowed to bring your own copy into the examination.

You will lose marks if you do not show all necessary work.

You may lose marks if you do not include appropriate units of measurement, where relevant.

You may lose marks if you do not give your answers in simplest form, where relevant.

Write the make and model of your calculator(s) here:

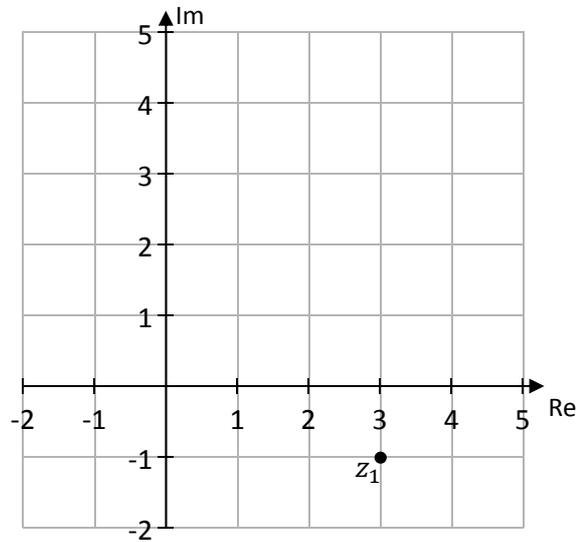
Question 2

(25 marks)

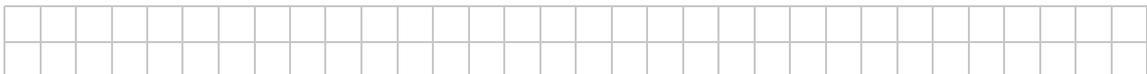
(a) The complex number $z_1 = a + bi$, where $i^2 = -1$, is shown on the Argand Diagram below.

(i) Write down the value of a and the value of b .

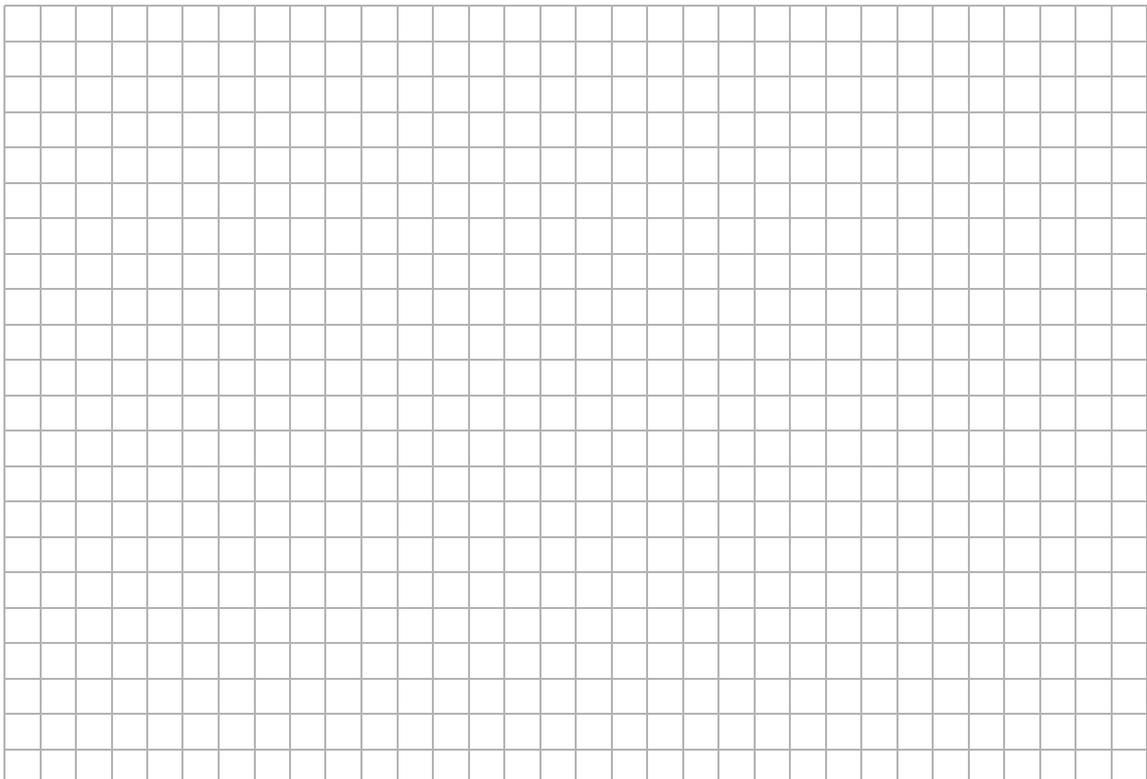
$a = \underline{\hspace{2cm}}$ $b = \underline{\hspace{2cm}}$



(ii) $z_2 = -1 + 2i$. Plot z_2 on the Argand Diagram.

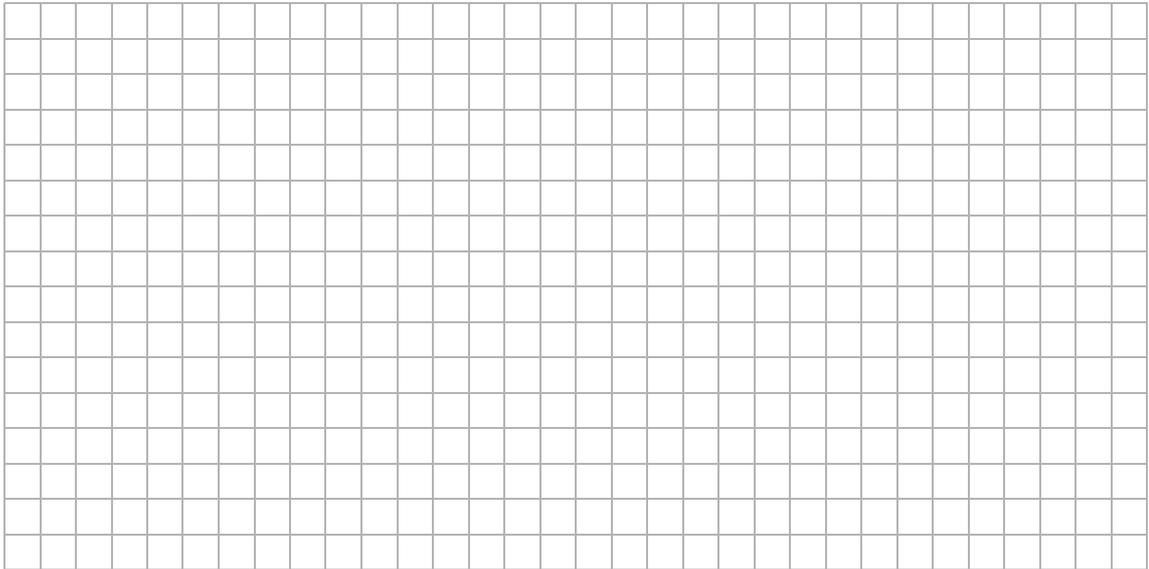


(iii) $z_3 = \frac{z_1}{z_2}$. Write z_3 in the form $x + yi$, where $x, y \in \mathbb{R}$.



(b) Solve for z :

$$2z - 6(4 - 6i) = (-1 + i)(4 - 2i).$$

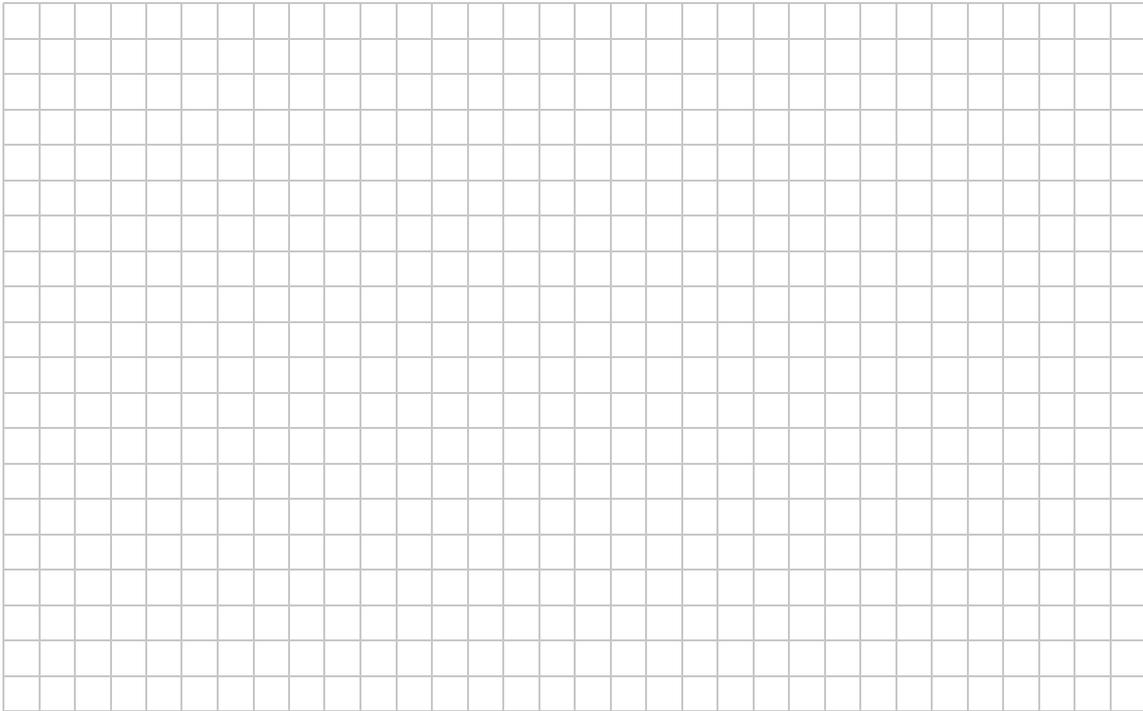


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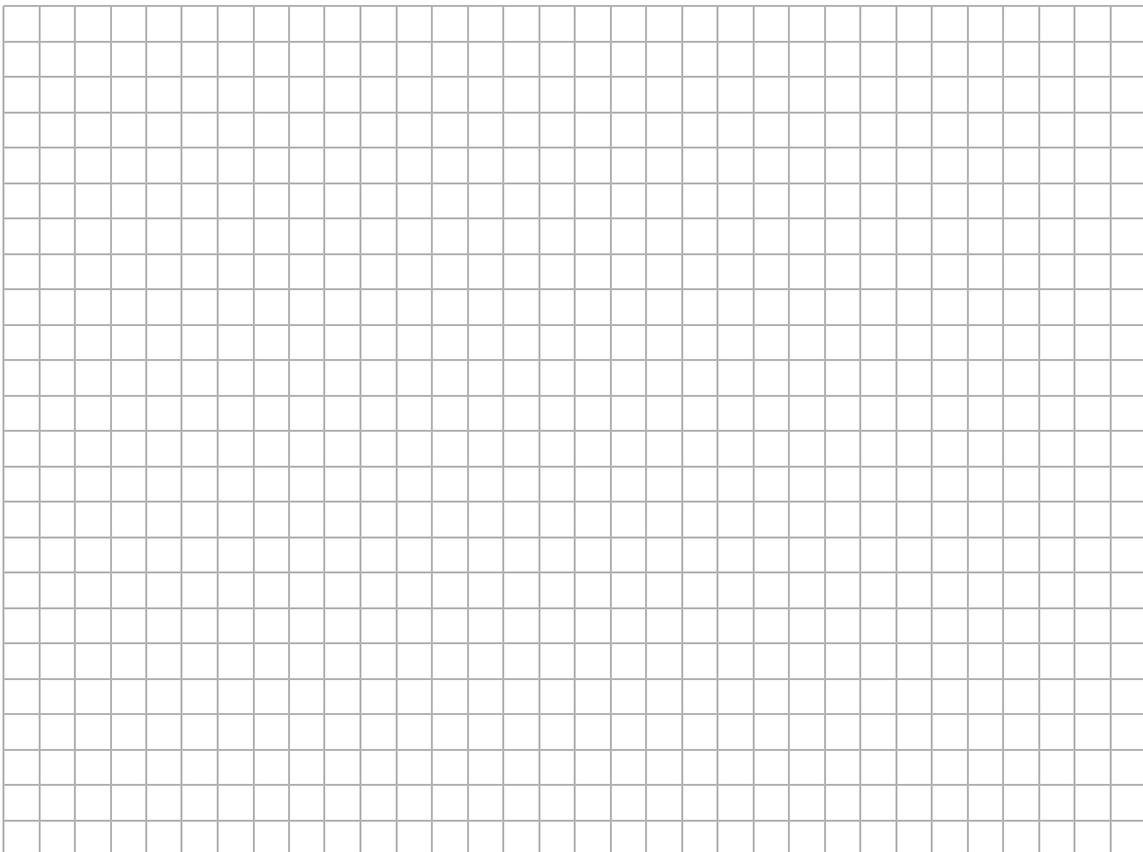
Question 3

(25 marks)

- (a) Find the two values of x for which $3x^2 - 6x - 8 = 0$.
Give each answer correct to 1 decimal place.



- (b) Find the co-ordinates of the minimum point of the function
 $f(x) = 3x^2 - 6x - 8$, where $x \in \mathbb{R}$.



Question 4

(25 marks)

(a) Solve for x :

$$11x - 5(2x - 1) = 3(6 - x) + 3.$$

(b) Solve the simultaneous equations:

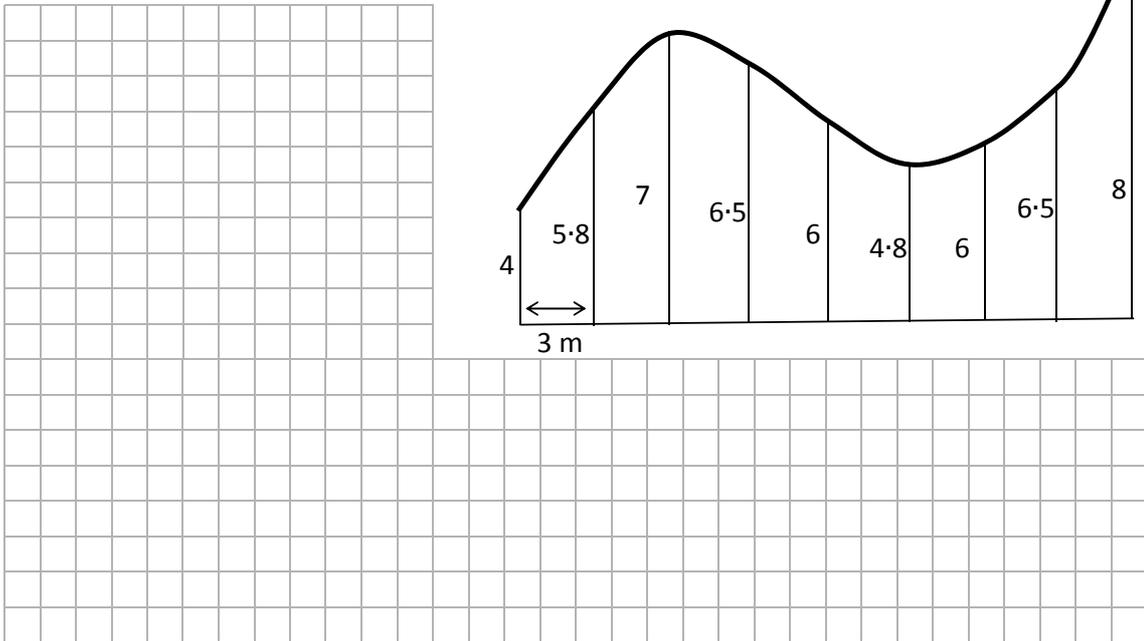
$$\begin{aligned} y + 5 &= 2x \\ x^2 + y^2 &= 25. \end{aligned}$$

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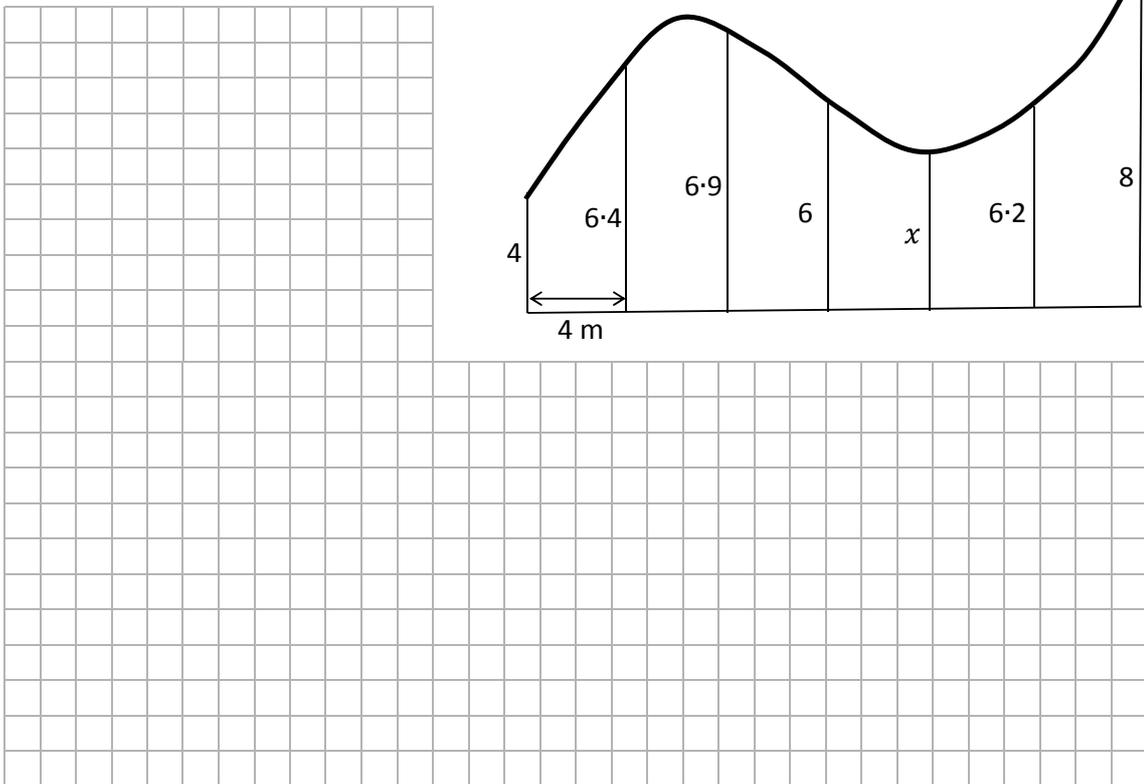
Question 5

(25 marks)

- (a) A field is divided into eight sections as shown below. The width of each section is 3 metres. The height, in metres, of each section is given in the diagram. Use the Trapezoidal rule to estimate the area of the field.



- (b) The area of the same field was re-estimated by applying the Trapezoidal rule again. This time, a different section width (4 m) and a different set of section heights were used, as shown below. The area was found to be 145.6 m^2 . Use this information to find the value of the height marked x on the diagram.



Question 6

(25 marks)

- (a) A salesman earns a basic salary of €150 per week. In addition, he gets commission of 20% on sales up to the value of €1000 in the week and 30% commission on any sales above this. Find his total income for a week when his total sales amount to €3000.

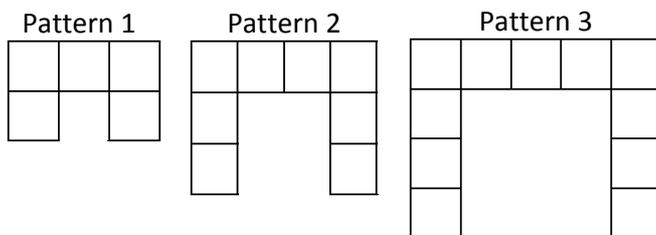
- (b) On a different week his total income is €1160. Find his total sales for this week.

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Answer **all three** questions from this section.

Question 7**(50 marks)**

The first three patterns in a sequence of patterns of tiles are shown in the diagram below.

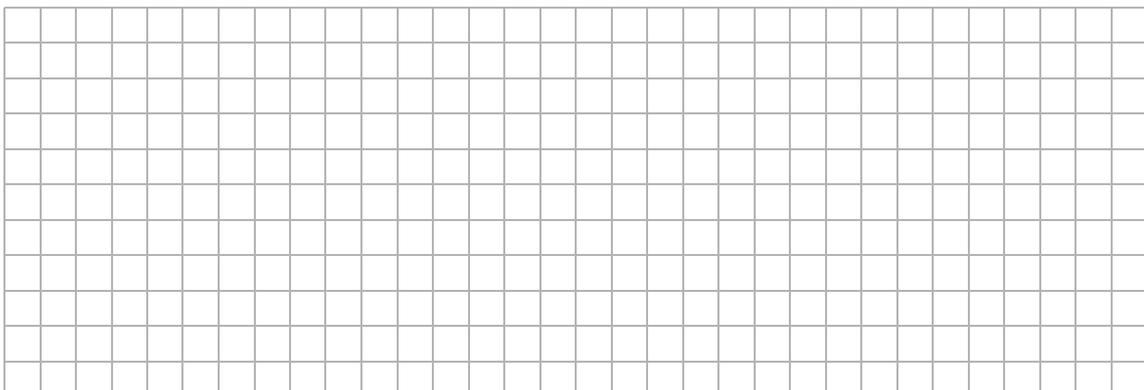


(a) Draw the next pattern of tiles onto the diagram above.

(b) Based on the patterns shown, complete the table below.

Pattern number (n)	Number of Tiles
1	5
2	
3	
4	
5	

(c) (i) Assuming the pattern continues, the number of tiles in the n^{th} pattern of the sequence is given by the formula $T_n = pn + q$, where p and $q \in \mathbb{N}$. Find the value of p and the value of q .



Question 9

(55 marks)

Forensic scientists can estimate the height of a person from the lengths of their bones. One method uses a function which relates the length of the femur bone, x , to the height of the person. Using this method the heights of males and females are estimated using the following functions:

Male: $m(x) = 2.3x + 65.53$,

where $m(x)$ is the height and x is the length of the femur, in cm.

Female: $f(x) = 2.5x + 54.13$,

where $f(x)$ is the height and x is the length of the femur, in cm.

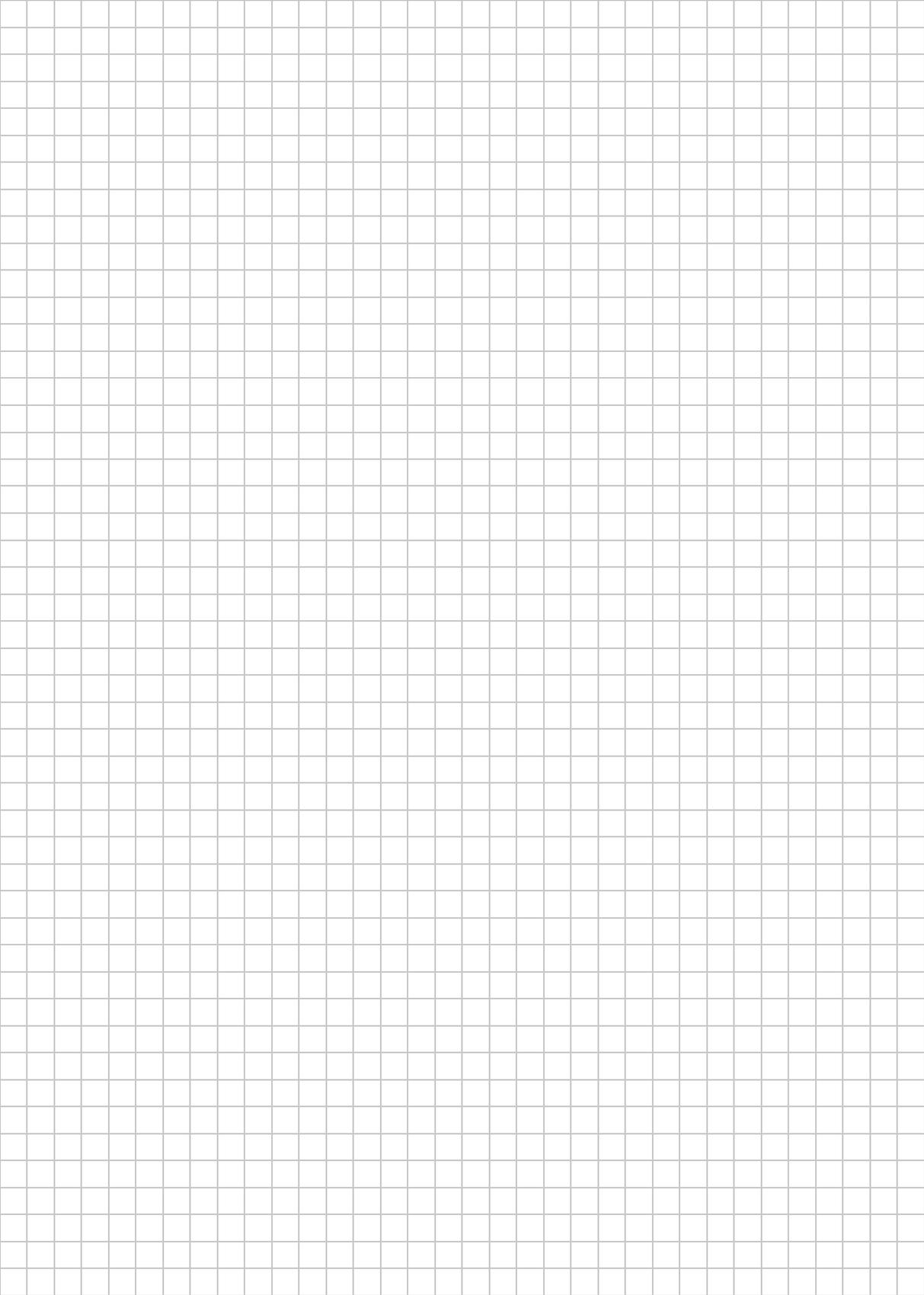
- (a) Use the functions above to estimate the height of a male and the height of a female each of whose femur is 47.54 cm in length. Give both answers correct to 2 decimal places.

Male height = <input style="width: 100%;" type="text"/>	Female height = <input style="width: 100%;" type="text"/>
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- (b) Use $m(x)$ to estimate the femur length of a male whose height is 184 cm. Give your answer correct to 2 decimal places.

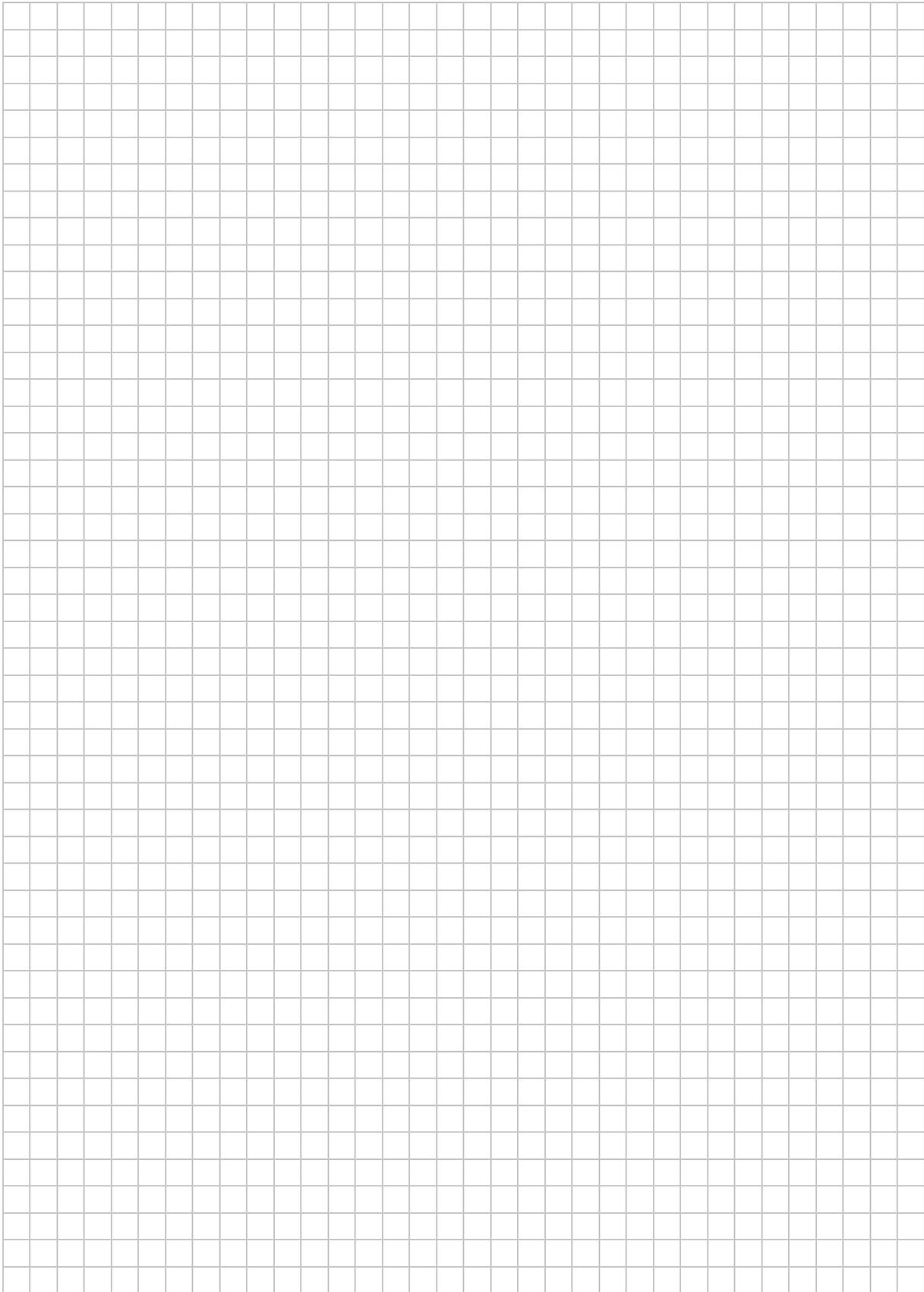
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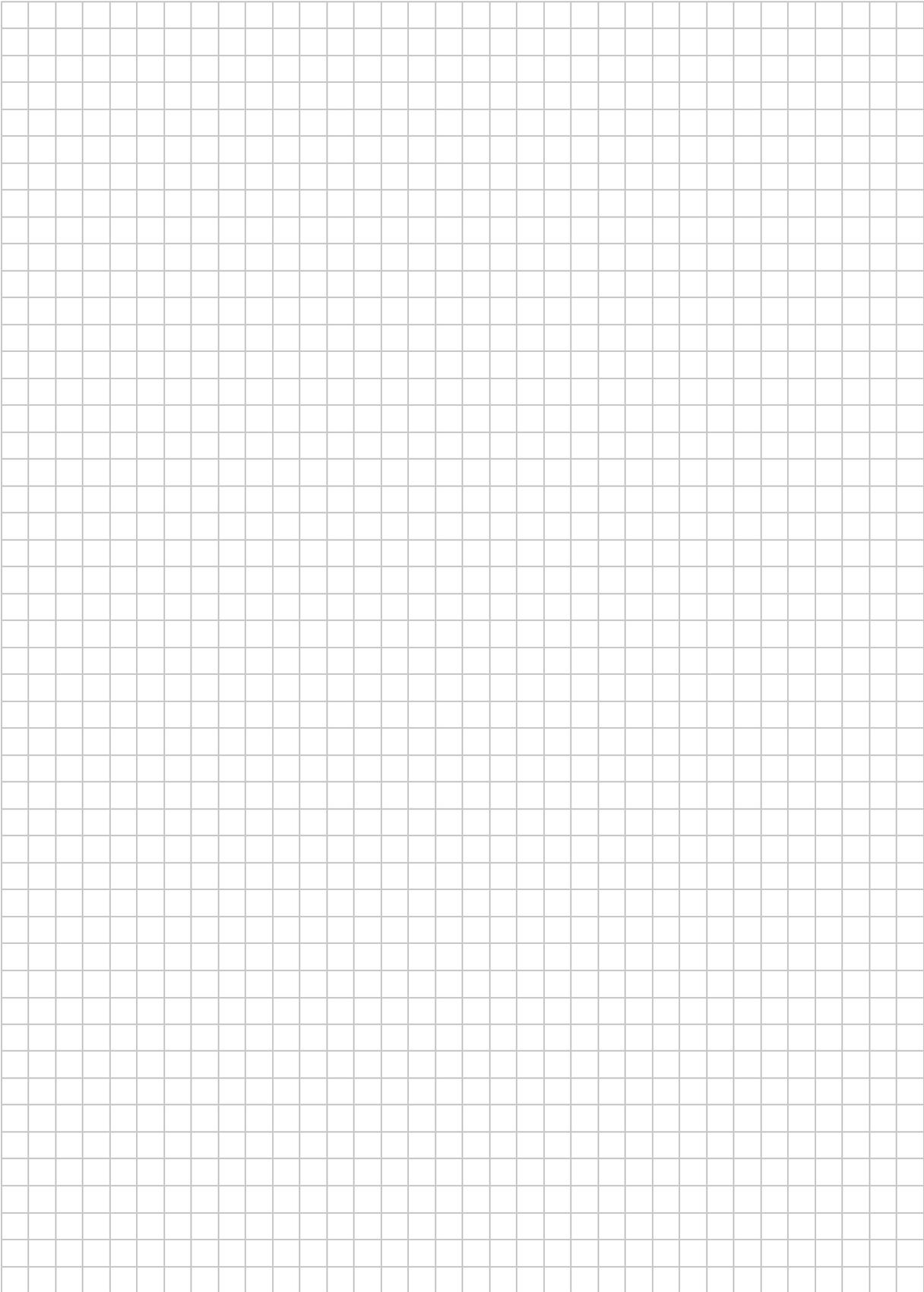


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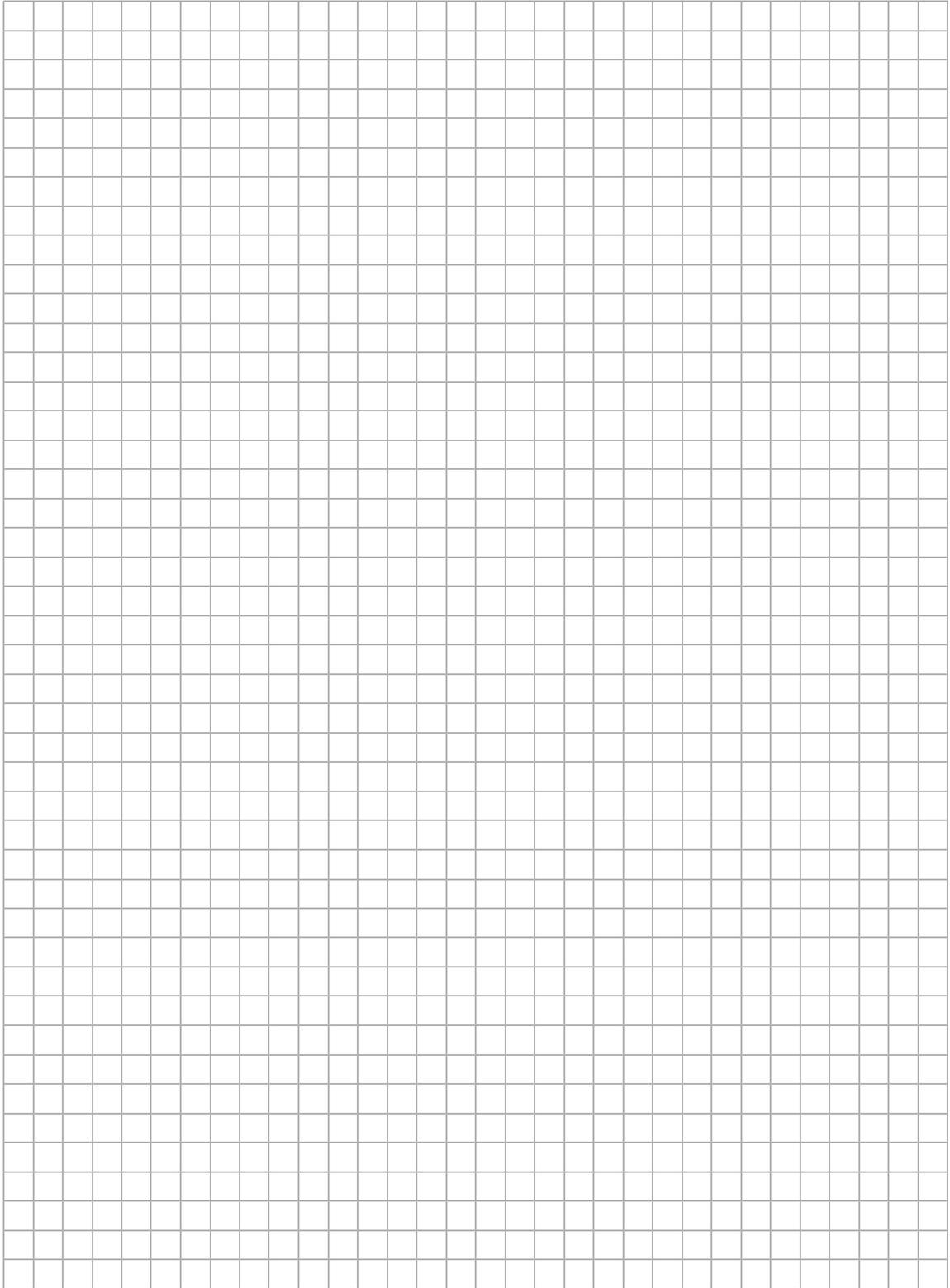
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Leaving Certificate 2017 - Ordinary Level

Mathematics – Paper 1

Friday 9 June

Afternoon 2:00 – 4:30